

Subject card

Subject name and code	Numerical Modeling of Dynamic Systems, PG_00174267						
Field of study	Mathematical Modeling and Data Analysis						
Date of commencement of studies	October 2023		Academic year of realisation of subject		2025/2026		
Education level	Bachelor's studies		Subject group				
Mode of study	full-time studies		Mode of delivery		at the university		
Year of study	3		Language of instruction		Polish		
Semester of study	5		ECTS credits		6.0		
Learning profile	academic		Assessment form		exam		
Conducting unit							
Name and surname of lecturer (lecturers)	Subject supervisor		dr Paweł Klinga				
	Teachers						
Lesson types	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	0.0	30.0	0.0	0.0	60
	E-learning hours included: 0.0						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan		Participation in consultation hours		Self-study	SUM
	Number of study hours	60		0.0		0.0	60
Subject objectives	The aim of the course is to introduce the subject of discrete dynamic systems.						
Learning outcomes	Course outcome		Subject outcome		Method of verification		
	[MMiADL3_U11] knows how to arrange and analyse an algorithm in accordance with the specification and save it in the selected programming language		Student addresses the methods presented during the lecture and, using Python, applies the algorithms in order to solve problems.		[SU2] presentation/project/paper/report		
	[MMiADL3_U10] is able to recognise problems, including practical issues, that can be solved algorithmically; can make a specification of such a problem		Student recognizes a given dynamic system and chooses an algorithm proper to analyze the issue.		[SU2] presentation/project/paper/report [SU4] test/exam - oral or written		
	[MMiADL3_W09] knows and understands the basics of computational and programming techniques supporting mathematician's work and understands their limitations		Student is able to analyze the behavior of a dynamic system using methods presented during the course.		[SW2] presentation/project/paper/report		
	[MMiADL3_K02] is ready to precisely formulate questions to deepen his/her own understanding of a given topic or to find missing elements of reasoning		By posing questions on a given problem, the student identifies areas that he/she is able to solve on his own and those in which he needs to deepen his knowledge.		[SK1] oral statement/conversation/discussion [SK8] observation of student's independent or team work		

Subject contents	Elementary recurrence relations and their solutions in Python		
	Leslie model of population distribution		
	Nonlinear dynamic systems: tent function, logistic map and their graphical iterations		
	Fixed points and periodic points of discrete dynamic systems and their stability		
	Bifurcation diagram, Lyapunov exponent		
	Complex dynamic systems, Julia and Mandelbrot sets		
	Fractals, fractal dimension		
Prerequisites and co-requisites			
Assessment methods and criteria	Subject passing criteria	Passing threshold	Percentage of the final grade
	Exam	51.0%	50.0%
	Project	51.0%	50.0%
Recommended reading	Basic literature	1. Stephen Lynch, <i>Dynamical Systems with Applications using Python</i> , Springer, 2018. 2. G.C. Layek, <i>An Introduction to Dynamical Systems and Chaos</i> , Springer, 2015.	
	Supplementary literature	adapted to the implemented project	
	eResources addresses		
Example issues/ example questions/ tasks being completed	Analysis of a population change in a given Leslie model		
	Analysis of a long-term behavior of a dynamic system given by a logistic map		
Work placement	Not applicable		

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